# The Crystal Structure of Barium Orthotitanate, $\mathbf{B a}_{\mathbf{2}} \mathbf{T i O}_{\mathbf{4}}$ 

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The crystal structure of $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ has been determined with moderate accuracy, using two-dimensional $F_{o}$ and $F_{o}-F_{c}$ syntheses. The space group is $P 2_{1} / n$ and the cell dimensions are:

$$
a_{0}=6 \cdot 12 \pm 0.03, b_{0}=7.70 \pm 0.03, c_{0}=10.50 \pm 0.03 \AA ; \beta=93^{\circ} 8^{\prime} \pm 10^{\prime}
$$

There are four units of $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ in the cell. The structure is of the $\beta-\mathrm{K}_{2} \mathrm{SO}_{4}$ type and is closely related to $\beta-\mathrm{Ca}_{2} \mathrm{SiO}_{4}$. The environment of the titanium atom is unusual; it is approximately tetrahedral and the structure is considered as an arrangement of discrete $\mathrm{TiO}_{4}$ groups and Ba atoms. The relationship between $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ and ferro-electric $\mathrm{BaTiO}_{3}$ is discussed.

## 1. Introduction

Barium orthotitanate, $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$, was first examined crystallographically by Rooksby (1947) who showed that its X-ray powder pattern resembles that of $\mathrm{Ba}_{2} \mathrm{SiO}_{4}$, which has the $\beta-\mathrm{K}_{2} \mathrm{SO}_{4}$ type of structure (O'Daniel \& Tscheischwili, 1942). Other workers (Rase \& Roy, 1955 ; Murray, 1958; Jonker \& Kwestroo, 1958) have prepared single-phase powders with composition $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ and have confirmed the observation of Rooksby.

The similarity between the powder patterns of the two compounds suggests that titanium in $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ may be compared with silicon in $\mathrm{Ba}_{2} \mathrm{SiO}_{4}$ and sulphur in $\beta-\mathrm{K}_{2} \mathrm{SO}_{4}$ and therefore may be tetrahedrally coordinated by four oxygen atoms. The present work was undertaken to determine the precise nature of the titanium coordination.

## 2. Experimental

## (i) Preparation of single crystals

Single crystals of $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ were grown from a melt containing $\mathrm{BaCl}_{2}, \mathrm{BaCO}_{3}$ and $\mathrm{TiO}_{2}$ in the ratio 5:5:1. This mixture was put in a platinum crucible and held at a temperature of $1340^{\circ} \mathrm{C}$. for 20 hr . and then cooled rapidly. The solidified flux was removed by solution in distilled water and the residue was quickly washed in alcohol. Approximately equal quantities of dark tan crystals and white crystals were found and these were separated by hand picking. The dark crystals were shown to be tetragonal $\mathrm{BaTiO}_{3}$. A powder photograph of some of the white crystals agreed closely with one published by Rase \& Roy (1955) for $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$. A spectrographic analysis of the white crystals showed barium and titanium as major constituents with traces of silicon, aluminium and platinum. A small quantity of these crystals was examined by Messrs. Johnson,

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Matthey and Co. Ltd., who found the composition to be:

| Ba | Ti | O |  |
| :---: | :---: | :---: | :---: |
| 66.72 | 15.24 | 17.65 | $\mathrm{wt} . \%$ |

It was assumed that this corresponds to $93.9 \%$ $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ and $6 \cdot 1 \% \mathrm{TiO}_{2}$.

## (ii) Unit cell and symmetry

A Buerger precession camera was used to determine the unit cell and symmetry of $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$; the cell was found to be monoclinic but pseudo-orthorhombic and pseudo-trigonal. The dimensions of the unit cell are given in Table 1 together with the cells of the closely related structures $\mathrm{Ba}_{2} \mathrm{SiO}_{4}$ and $\beta-\mathrm{Ca}_{2} \mathrm{SiO}_{4}$ (Midgley, 1952). A careful scrutiny of precession and oscillation photographs was carried out to make quite sure that the axial lengths are not doubled, as it is for some of the polymorphic modifications of $\mathrm{Ca}_{2} \mathrm{SiO}_{4}$ (Douglas, 1952). Reflexions were observed in the $h 0 l$ zone only with $(h+l)$ even and in the $0 k 0$ zone only with $k$ even, which are consistent with the space-group $P 2_{1} / n$. The choice of axes is unconventional but is convenient for

Table 1. Unit-cell constants of $\mathrm{Ba}_{2} \mathrm{TiO}_{4}, \mathrm{Ba}_{2} \mathrm{SiO}_{4}$ and

$$
\beta-\mathrm{Ca}_{2} \mathrm{SiO}_{4}
$$ $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$

Monoclinic, $P 2_{1} / n$
$a=6.12 \pm 0.03, b=7.70 \pm 0.03, c=10.50 \pm 0.03 \AA$ $a: b=0.792, b: c=0.733, \beta=93^{\circ} 8^{\prime} \pm 10^{\prime}$
$\mathrm{Ba}_{2} \mathrm{SiO}_{4}$
(O'Daniel \& Tscheischwili, 1942)
$a=5.77, b=7.57, c=10.19 \AA$
$a: b=0.762, b: c=0.743$
$\beta-\mathrm{Ca}_{2} \mathrm{SiO}_{4}$ (Midgley, 1952) Monoclinic, $P 2_{1} / n$
$a=5 \cdot 48 \pm 0.02, b=6.76 \pm 0.02, c=9.28 \pm 0.02 \AA$
$a: b=0.810, b: c=0.729, \beta=94^{\circ} 33^{\prime}$

[^0] given.
comparison with the $\beta-\mathrm{Ca}_{2} \mathrm{SiO}_{4}$ structure. All crystals examined were twinned on (100) or (001).

The density calculated on the basis of four units of $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ per cell was found to be $5 \cdot 16 \mathrm{~g} . \mathrm{cm} .^{-3}$, which may be compared with an observed value of $5 \cdot 07 \pm 0 \cdot 15$ g.cm. ${ }^{-3}$, obtained by the displacement method.

## (iii) $X$-ray intensities

Intensity data in the $h k 0,0 k l$ and $h 0 l$ zones were collected using a Weissenberg camera and Mo $K \alpha$ radiation; visual estimates of the intensities were made by comparison with a standard scale and corrections for Lorentz and polarization factors were made in the usual way. The crystal was roughly cubic in shape with edges of about 0.1 mm . and consisted of a twin with two components in the ratio $2 \cdot 45$ : l. Reflexions from one component were absorbed in the other component but no correction was made for this effect. It was found, however, that there was an agreement factor of $7 \%$ between structure factors obtained independently from the two components.

## 3. Approximate structure

Patterson syntheses were prepared for the three axial projections using a sharpening function of the type advocated by Lipson \& Cochran (1953). It was assumed that the strongest peaks in the syntheses correspond to $\mathrm{Ba}-\mathrm{Ba}$ and $\mathrm{Ba}-\mathrm{Ti}$ vectors and a selfconsistent set of position coordinates was obtained for the two independent Ba atoms and the Ti atom. The coordinates are listed in Table 2 together with the coordinates of corresponding atoms in $\beta-\mathrm{Ca}_{2} \mathrm{SiO}_{4}$. It is evident that if the $x$-axis of $\beta$ - $\mathrm{Ca}_{2} \mathrm{SiO}_{4}$ is reversed then the heavier atoms in the two structures occupy similar positions.

Table 2. Atomic co-ordinates derived from Patterson syntheses, compared with the atomic co-ordinates in $\beta-\mathrm{Ca}_{2} \mathrm{SiO}_{4}$

|  |  | $x$ | $y$ | $z$ |
| :---: | :--- | :---: | :---: | :---: |
|  |  |  |  |  |
| $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ | $\mathrm{Ba}_{\mathbf{I}}$ | 0.767 | 0.850 | 0.067 |
|  | $\mathrm{Ba}_{\text {II }}$ | 0.227 | 0.492 | 0.195 |
|  | Ti | 0.767 | 0.292 | 0.063 |
|  |  | $x$ |  |  |
|  |  | $y$ | $z$ |  |
| $\beta-\mathrm{Ca}_{2} \mathrm{SiO}_{4}$ | $\mathrm{Ca}_{\mathrm{I}}$ | -0.760 | 0.838 | 0.071 |
|  | $\mathrm{Ca}_{\text {II }}$ | -0.216 | 0.502 | 0.201 |
|  | Si | -0.760 | 0.276 | 0.071 |

At this stage in the analysis it was possible to predict certain features of the arrangement of oxygen atoms by considering the coordinates in Table 2 and by noting that the normal $\mathrm{Ti}-\mathrm{O}$ distance found in other structures is about $2 \cdot 0 \AA$. The shortest distance between two Ti atoms is about $5 \cdot 5 \AA$ which means that one oxygen atom cannot be in contact with two titanium neighbours. It follows that the polyhedron of oxygen atoms surrounding one titanium atom will be isolated from that surrounding a neighbouring
titanium atom. Since there is only one titanium atom in the asymmetric unit, all polyhedra surrounding titanium will be identical, so that if the $\mathrm{Ti}: \mathrm{O}$ ratio of $1: 4$ is to be preserved, the number of oxygen atoms in each polyhedron cannot exceed four. We may conclude that the titanium atom in $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ cannot be octahedrally coordinated by oxygen.

## 4. Refinement of the structure

## (i) Scattering curves

The scattering curves used in the refinement process were derived from the published values in the Internationale Tabellen (1935). It was assumed that barium is in the ionized state $\mathrm{Ba}^{2+}$ and the corresponding


Fig. 1. Final $F_{o}$ synthesis on (100). The contours are drawn at intervals approximately equal to 5 e. $\AA^{-2}$ for the heavy atoms and 2.5 e. $\AA^{-2}$ for the oxygen atoms. The point $P$ marks an alternative position for $\mathrm{O}_{\mathrm{IV}}$ suggested by packing considerations.


Fig. 2. Partial difference synthesis on ( 001 ) showing electron density due to oxygen atoms with contours drawn at intervals approximately equal to $2.5 \mathrm{e} \AA^{-2}$. The point $P$ marks an alternative position for $\mathrm{O}_{I V}$ suggested by packing considerations.

Table 3(a). Observed and calculated structure factors

| hkl | $F_{0}$ | $F_{c}$ | $F_{c}^{\prime}$ | $h k l$ | $F_{0}$ | $F_{c}$ | $F_{c}^{\prime}$ | hkl | $F_{0}$ | $F_{c}$ | $F_{c}^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 002 |  | 5 | 0 | 035 | 55 | -62 | -51 | 066 | 73 | -66 | -72 |
| 004 | 60 | -28 | -41 | 036 | $<30$ | 15 | 15 | 067 | $<37$ | -12 | -10 |
| 006 | 128 | $-134$ | -149 | 037 | 180 | 220 | 231 | 068 | 136 | -145 | -150 |
| 008 | 220 | -244 | -255 | 038 | <34 | -18 | -22 | 069 | <41 | -7 | -2 |
| 0,0,10 | 124 | 117 | 111 | 039 | <34 | 10 | 18 | 0,6,10 | 85 | 87 | 84 |
| 0,0,12 | <40 | 29 | 30 | 0,3,10 | 53 | -48 | -52 |  |  |  |  |
| 0,0,14 | 128 | 151 | 140 | 0,3,11 | 56 | -59 | -57 | 071 | 80 | 66 | 66 |
|  |  |  |  | 0,3,12 | <40 | -12 | -17 | 072 | 85 | 67 | 67 |
| 011 | $<20$ | 27 | 27 |  |  |  |  | 073 | 106 | 120 | 117 |
| 012 | 45 | 46 | 51 | 040 | 150 | 112 | 112 | 074 | 80 | 93 | 93 |
| 013 | 136 | 159 | 154 | 041 | 76 | -42 | -43 | 075 | 176 | -186 | -193 |
| 014 | 111 | 139 | 145 | 042 | 183 | -179 | -176 | 076 | $<39$ | 19 | 19 |
| 015 | 153 | -201 | -209 | 043 | 144 | -148 | -151 | 077 | $<40$ | -7 | -14 |
| 016 | 37 | 36 | 37 | 044 | 66 | 54 | 61 | 078 | 30 | -47 | -47 |
| 017 | 58 | 71 | 63 | 045 | 110 | -108 | -110 | 079 | 46 | -63 | -69 |
| 018 | 45 | -47 | -52 | 046 | 88 | 79 | 88 | 0,7,10 | 65 | -73 | -73 |
| 019 | 68 | -73 | -78 | 047 | 45 | 33 | 35 |  |  |  |  |
| 0,1,10 | 50 | -49 | -58 | 048 | 70 | -61 | -53 | 080 | 118 | 109 | 109 |
| 0,1,11 | $<38$ | 4 | 3 | 049 | 98 | 90 | 94 | 081 | 53 | 53 | 54 |
| 0,1,12 | 45 | -32 | -42 | 0,4,10 | 104 | 107 | 111 | 082 | 108 | -83 | -84 |
| 0,1,13 | 113 | 111 | 110 | 0,4,11 | 83 | 72 | 77 | 083 | 55 | 68 | 70 |
|  |  |  |  | 0,4,12 | 99 | -105 | -106 | 084 | 55 | 45 | 43 |
| 020 | $<18$ | 28 | 28 |  |  |  |  | 085 | 30 | 51 | 52 |
| 021 | 93 | 80 | 84 | 051 | 55 | -37 | -37 | 086 | $<42$ | 22 | 19 |
| 022 | 168 | -203 | -202 | 052 | 133 | -145 | -148 | 087 | $<43$ | 6 | 4 |
| 023 | 133 | 185 | 192 | 053 | 103 | 85 | 86 | 088 | 88 | -71 | -75 |
| 024 | 108 | 111 | 113 | 054 | 136 | -133 | -137 | 089 | 65 | -61 | $-66$ |
| 025 | 121 | 132 | 136 | 055 | 118 | - 120 | -118 |  |  |  |  |
| 026 | 116 | 96 | 99 | 056 | 48 | -56 | -56 | 091 | 153 | -140 | -139 |
| 027 | $<30$ | -21 | -26 | 057 | 100 | 106 | 108 | 092 | 58 | 34 | 36 |
| 028 | 45 | -31 | -30 | 058 | 90 | 78 | 83 | 093 | 58 | 53 | 54 |
| 029 | 95 | -103 | -114 | 059 | 38 | -54 | -53 | 094 | $<40$ | 51 | 53 |
| 0,2,10 | 98 | 102 | 104 | 0,5,10 | 113 | 110 | 119 | 095 | $<43$ | -4 | -3 |
| 0,2,11 | 95 | -74 | -85 |  |  |  |  | 096 | $<44$ | 2 | 2 |
| 0,2,12 | 118 | -148 | -148 | 060 | 257 | 250 | 250 | 097 | 150 | 177 | 179 |
|  |  |  |  | 061 | <32 | -10 | -12 |  |  |  |  |
| 031 | 200 | -240 | -240 | 062 | <33 | -28 | -30 | 0,10,0 | <44 | 18 | 18 |
| 032 | 90 | 85 | 88 | 063 | $<34$ | -19 | -22 | 0,10,1 | $<44$ | -3 | -3 |
| 033 | 121 | 114 | 119 | 064 | <34 | 12 | 8 | 0,10,2 | 125 | -118 | -117 |
| 034 | 63 | 51 | 53 | 065 | $<35$ | -2 | -4 | 0,10,3 | $<41$ | -30 | -29 |

The $F_{c}^{\prime}$ values are based on the structure which has $\mathrm{O}_{\mathrm{IV}}$ in the alternative position $\mathrm{O}_{\mathrm{IV}}^{\prime}$.
The $<$ sign indicates an unobserved reflexion; the corresponding value of $F_{o}$ is the minimum observable $F_{o}$ in that region of the photograph.
curve was obtained by drawing a smooth line from the curve for Ba at $\sin \theta / \lambda=0.3$ to the value 54 at $\sin \theta / \lambda=0$. The curve $\mathrm{Ti}^{+4}$ was used for titanium and the curve $\mathbf{0}^{-2}$ was used for oxygen. In the final stages of the structure determination, temperature factors of the form $\exp \left(-B \sin ^{2} \theta / \lambda^{2}\right)$ were applied to scattering curves with $B=0.25 \AA^{2}, 0 \cdot 40 \AA^{2}$ and $0 \cdot 40 \AA^{2}$ for barium, titanium and oxygen respectively.

## (ii) The (100) and (001) projections

Refinement was carried out using the $0 k l$ and $h k 0$ intensity data; reflexions with $\sin \theta / \lambda<0 \cdot 4$ were considered first and higher angle reflexions included at later stages. The signs of the $F_{c}$ values, obtained by considering heavy atoms only, were applied to the observed structure factors and the corresponding $F_{o}$ and $F_{o}-F_{c}$ syntheses were calculated. After a few cycles, peaks corresponding to oxygen atoms were detected and their contribution was included in subsequent structure factor calculations.

The final $F_{o}$ synthesis on (100) is shown in Fig. 1 with a converging factor $\exp \left[-1.8 \sin ^{2} \theta / \lambda^{2}\right]$ applied to the Fourier coefficients. In this projection, $\mathrm{O}_{\mathrm{I}}$ is well resolved, $O_{\text {II }}$ and $O_{\text {IV }}$ overlap slightly with each other and $\mathrm{O}_{\text {IV }}$ is partly obscured by $\mathrm{Ba}_{\mathrm{I}}$. On the (001) projection, however, the oxygen atoms are well separated from each other and are shown in the partial difference synthesis obtained after the heavy atoms had been removed (Fig. 2). On completion of the refinement, an $R$-factor of approximately $14 \%$ was obtained on each projection; $F_{o}$ values were scaled for comparison with $F_{c}$ and unobserved reflexions were included when $F_{c}$ exceeded the minimum observable level. Values of $F_{o}$ and $F_{c}$ for the $0 k l$ an $h k 0$ reflexions are given in Tables $3(a)$ and $3(b)$ respectively. The corresponding atomic coordinates are given in Table 4. The standard deviations quoted in Table 4 were obtained by assuming that the standard deviation in the $F_{o}$ values is $15 \%$ of $F_{o}$ (Lipson \& Cochran, 1953). The corresponding standard deviations in the interatomic distances are then approximately $0.17 \AA$ for

Table 3(b). Observed and calculated structure factors

| $h k l$ | $F_{o}$ | $F_{c}$ | $F_{c}^{\prime}$ | hkl | $F_{0}$ | $F_{c}$ | $F_{c}^{\prime}$ | $h k l$ | $F_{0}$ | $F_{c}$ | $F_{c}^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 200 | 360 | -416 | -428 | 930 | 122 | -137 | -137 | 670 | <43 | -35 | -36 |
| 400 | 260 | 299 | 313 |  |  |  |  | 770 | $<44$ | 14 | 23 |
| 600 | 198 | -191 | -194 | 040 | 128 | 112 | 112 |  |  |  |  |
| 800 | 154 | 129 | 121 | 140 | 147 | 146 | 145 | 080 | 96 | 109 | 109 |
|  |  |  |  | 240 | 96 | -79 | -72 | 180 | 78 | -61 | -60 |
| 110 | <18 | -30 | -26 | 340 | 146 | -139 | -134 | 280 | 103 | -105 | $-107$ |
| 210 | 64 | -62 | -56 | 440 | 87 | 68 | 58 | 380 | 71 | 54 | 49 |
| 310 | 72 | 72 | 71 | 540 | 103 | 98 | 94 | 480 | 60 | 67 | 71 |
| 410 | 56 | 36 | 40 | 640 | 55 | -44 | -41 | 580 | 63 | -59 | -54 |
| 510 | 46 | -52 | -59 | 740 | 62 | -76 | -77 | 680 | $<43$ | -56 | -57 |
| 610 | 51 | -46 | -56 |  |  |  |  |  |  |  |  |
| 710 | 57 | 51 | 58 | 150 | <28 | -13 | - 14 | 190 | $<39$ | -30 | -31 |
| 810 | $<40$ | 46 | 53 | 250 | <29 | 25 | 21 | 290 | <40 | -21 | -19 |
|  |  |  |  | 350 | 72 | 57 | 57 | 390 | <41 | 60 | 60 |
| 020 | $<18$ | 28 | 28 | 450 | <32 | -51 | -55 | 490 | <41 | 21 | 23 |
| 120 | 163 | -164 | -161 | 550 | 53 | -53 | -51 | 590 | 65 | -90 | -89 |
| 220 | 93 | -90 | -87 | 650 | $<41$ | 40 | 50 | 690 | $<48$ | 20 | 18 |
| 320 | 148 | $-156$ | -143 | 750 | <43 | 72 | 71 |  |  |  |  |
| 420 | $<27$ | 25 | 21 |  |  |  |  | 0,10,0 | $<43$ | 18 | 18 |
| 520 | 115 | -114 | -106 | 060 | 235 | 250 | 250 | 1,10,0 | <45 | 41 | 42 |
| 620 | $<37$ | -7 | -6 | 160 | $<32$ | 16 | 15 | 2,10,0 | $<47$ | -11 | -9 |
| 720 | 92 | 82 | 85 | 260 | 213 | -223 | -227 | 3,10,0 | $<48$ | -27 | -28 |
| 820 | <45 | -10 | -8 | 360 | $<33$ | -7 | -4 | 4,10,0 | < 50 | 16 | 11 |
| 920 | $<48$ | -49 | -58 | 460 | 180 | 178 | 183 |  |  |  |  |
|  |  |  |  | 560 | $<39$ | 19 | 15 | 1,11,0 | $<45$ | 0 | -1 |
| 130 | 62 | -46 | -51 | 660 | 114 | -107 | -113 | 2,11,0 | $<48$ | 14 | 13 |
| 230 | <22 | -5 | -2 | 760 | $<44$ | -2 | -4 | 3,11,0 | < 50 | 41 |  |
| 330 | 96 | 83 | 84 | 860 | 52 | 80 | 76 | 4,11,0 | $<52$ | 22 |  |
| 430 | 25 | 27 | 29 |  |  |  |  |  |  |  |  |
| 530 | 137 | -143 | -134 | 170 | $<33$ | -13 | -10 | 0,12,0 | 135 | 139 |  |
| 630 | $<37$ | -11 | -15 | 270 | $<35$ | -15 | -15 | 1,12,0 | 72 | -72 |  |
| 730 | 137 | 134 | 124 | 370 | $<37$ | 29 | 28 | 2,12,0 | 103 | -129 |  |
| 830 | < 45 | 11 | 14 | 470 | $<39$ | 39 | 39 | 3,12,0 | 52 | 72 |  |
|  |  |  |  | 570 | $<41$ | -34 | -41 | 4,12,0 | 75 | 99 |  |

The $F_{c}^{\prime}$ values are based on the structure which has $\mathrm{O}_{\mathrm{IV}}$ in the alternative position $\mathrm{O}_{\mathrm{I} v}^{\prime}$.
The < sign indicates an unobserved reflexion; the corresponding value of $F_{o}$ is the minimum observable $F_{o}$ in that region of the photograph.
the metal-oxygen distances and $0.22 \AA$ for the oxygenoxygen distances. It is estimated that the standard deviation for interbond angles is of the order of $5^{\circ}$.

Table 4. Final atomic co-ordinates and standard deviations in $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$

|  | $x$ | $y$ | $z$ |
| :--- | :---: | :---: | :---: |
| $\mathrm{Ba}_{\mathrm{I}}$ | 0.765 | 0.841 | 0.076 |
| $\mathrm{Ba}_{\text {II }}$ | 0.229 | 0.498 | 0.202 |
| Ti | 0.754 | 0.276 | 0.079 |
| $\mathrm{O}_{\mathrm{I}}$ | 0.693 | 0.008 | 0.430 |
| $\mathrm{O}_{\text {II }}$ | 0.567 | 0.230 | 0.180 |
| $\mathrm{O}_{\text {III }}$ | 0.993 | 0.190 | 0.153 |
| $\mathrm{O}_{\mathrm{IV}}$ | 0.650 | 0.145 | 0.970 |
| $\mathrm{O}_{\mathrm{IV}}^{\prime}$ | $(0.695)$ | $(0.145)$ | $(0.945)$ |
|  | $\sigma(x)$ for | $\mathrm{Ba}=0.01 \AA$ |  |
|  | $\sigma(x)$ for | $\mathrm{Ti}=0.05$ |  |
|  | $\sigma(x)$ for | O | $=0.16$ |

These coordinates were obtained by Fourier methods except for $\mathrm{O}_{\mathrm{I}}^{\prime}$ which is an alternative position for $\mathrm{O}_{\mathrm{IV}}$ obtained by packing considerations.

## 5. Description of the structure

The results of the structure analysis show that Rooksby's (1947) suggestion is correct and that
$\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ has the $\beta-\mathrm{K}_{2} \mathrm{SO}_{4}$ type of structure and the titanium atom is surrounded by a distorted tetrahedron of oxygen atoms (Fig. 5). The structure may be regarded as a sequence of $\mathrm{TiO}_{4}$ groups which alternate with the $\mathrm{Ba}_{\mathrm{I}}$ atoms in the $y$-direction. These strings of barium atoms and tetrahedra are linked through the $\mathrm{Ba}_{\text {II }}$ atoms which are located between the tetrahedra. There is a pseudo-trigonal arrangement of tetrahedra about the $\mathrm{Ba}_{\text {II }}$ atoms. The structure is not strictly isomorphous with $\beta-\mathrm{Ca}_{2} \mathrm{SiO}_{4}$ but there is a close correspondence between the atomic positions. This is illustrated in Figs. 3 and 4 which represent projections of the two structures on (100) and (001) respectively; corresponding $\mathrm{SiO}_{4}$ and $\mathrm{TiO}_{4}$ tetrahedra are outlined.

The interatomic distances are listed in Table 5(a). Although the standard deviations indicate a large range of uncertainty in any one distance, it does appear that the Ti-O bonds are abnormally short when compared with $1.86 \AA$, which is the sum of the Goldschmidt radii corrected for the reduction of the coordination number from six to four (Pauling, 1940). The $\mathrm{Ti}-\mathrm{O}$ bond in $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ must therefore have a considerable covalent character. The angles between the bonds, (Table $5(b)$ ), range from $94^{\circ}$ to $129^{\circ}$, which


Fig. 3. Diagrammatic projections of (a) $\beta-\mathrm{Ca}_{2} \mathrm{SiO}_{4}$ and (b) $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ on (100) showing the close similarity between the structures. Corresponding oxygen tetrahedra are outlined.


Fig. 4. Diagrammatic projections of (a) $\beta-\mathrm{Ca}_{2} \mathrm{SiO}_{4}$ and (b) $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ on (001) showing the close similarity between structures. Corresponding oxygen tetrahedra are outlined.


Fig. 5. A stereogram showing the approximately tetrahedral arrangement of oxygen atoms round the titanium atom. The point $P$ marks an alternative position for $O_{\text {IV }}$ suggested by packing considerations.
deviate from the normal tetrahedral angle of $109^{\circ} 28^{\prime}$; a stereogram of the distorted tetrahedron is shown in Fig. 5. The oxygen-oxygen distances within the tetrahedron lie reasonably close to the normal value of $2.8 \AA$ with the exception of the short distance of $2.38 \AA$ between $\mathrm{O}_{\text {II }}$ and $\mathrm{O}_{\text {IV }}$. It was found that when

Table 5(a). Interatomic distances in $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$

| Atom | No. of neighbours | Neigh bour | Distance |
| :---: | :---: | :---: | :---: |
| Ti* | 4 | $\mathrm{O}_{\text {IV }}$ | 1.63 A |
|  |  | $\mathrm{O}_{\text {II }}$ | $1 \cdot 64$ |
|  |  | $\mathrm{O}_{\text {III }}$ | 1.75 |
|  |  | $\mathrm{O}_{\mathrm{I}}$ | $1 \cdot 82$ |
| $\mathrm{O}_{\mathrm{I}}$ |  | $\mathrm{O}_{\text {III }}$ | $2 \cdot 82$ |
|  |  | $\mathrm{O}_{\mathrm{I}}$ | $2 \cdot 85$ |
|  |  | $\mathrm{O}_{\text {IV }}$ | 3•12 |
|  |  | $\mathrm{O}_{\text {II }}$ | $2 \cdot 87$ |
| $\mathrm{O}_{\text {II }}$ |  | $\mathrm{O}_{\text {IV }}$ | 2.38 |
|  |  | $\mathrm{O}_{\text {III }}$ | $2 \cdot 66$ |
| $\mathrm{O}_{\text {III }}$ |  | $\mathrm{O}_{\text {IV }}$ | $2 \cdot 79$ |
| $\mathrm{O}_{\text {IV }}$ |  | $\mathrm{O}_{\text {IV }}$ | 2.98 |
| $\mathrm{Ba}_{\text {I }}$ | 9 or 10 | $\mathrm{O}_{\text {IV }}$ | $2 \cdot 56$ |
|  |  | $\mathrm{O}_{\mathrm{I}}$ | 2.58 |
|  |  | $\mathrm{O}_{\text {IV }}$ | $2 \cdot 67$ |
|  |  | $\mathrm{O}_{\text {II }}$ | $2 \cdot 84$ |
|  |  | $\mathrm{O}_{\text {III }}$ | $2 \cdot 90$ |
|  |  | $\mathrm{O}_{\text {III }}$ | $3 \cdot 11$ |
|  |  | $\mathrm{O}_{\text {III }}$ | $3 \cdot 32$ |
|  |  | $\mathrm{O}_{\text {II }}$ | $3 \cdot 43$ |
|  |  | $\mathrm{O}_{\text {III }}$ | $3 \cdot 52$ |
|  |  | $\mathrm{O}_{\text {IV }}$ | $3 \cdot 64$ |
| Ba ${ }_{\text {II }}$ | 8 | $\mathrm{O}_{\text {III }}$ | $2 \cdot 67$ |
|  |  | $\mathrm{O}_{\text {III }}$ | $2 \cdot 81$ |
|  |  | $\mathrm{O}_{1}$ | $2 \cdot 85$ |
|  |  | $\mathrm{O}_{\mathrm{I}}$ | $2 \cdot 87$ |
|  |  | $\mathrm{O}_{\text {II }}$ | $2 \cdot 87$ |
|  |  | $\mathrm{O}_{\text {II }}$ | 2.94 |
|  |  | OIV | $3 \cdot 08$ |
|  |  | OIV | $3 \cdot 39$ |

Standard deviations of bond lengths
Metal-oxygen $0.17 \AA \quad$ Oxygen-oxygen $0.22 \AA$

* The next greatest $\mathrm{Ti}-\mathrm{O}$ distance is $3,59 \AA$ to $\mathrm{O}_{\mathrm{I}}$ in a neighbouring tetrahedron.

Table 5(b). Angles in the $\mathrm{TiO}_{4}$ tetrahedron

| $\mathrm{O}_{\mathrm{I}}-\mathrm{Ti}-\mathrm{O}_{\mathrm{IV}}$ | $129^{\circ}$ |
| :--- | ---: |
| $\mathrm{O}_{\mathrm{II}} \mathrm{Ti}-\mathrm{O}_{\mathrm{IV}}$ | 94 |
| $\mathrm{O}_{\mathrm{III}}-\mathrm{Ti}-\mathrm{O}_{\mathrm{II}}$ | 103 |
| $\mathrm{O}_{\mathrm{III}}-\mathrm{Ti}-\mathrm{O}_{\mathrm{I}}$ | 104 |
| $\mathrm{O}_{\mathrm{I}}-\mathrm{Ti}-\mathrm{O}_{\mathrm{II}}$ | 112 |
| $\mathrm{O}_{\mathrm{III}}-\mathrm{Ti}-\mathrm{O}_{\mathrm{IV}}$ | 111 |

$\mathrm{O}_{\text {IV }}$ was shifted from position ( $0.650,0 \cdot 145,0.970$ ) to ( $0.695,0.145,0.945$ ), shown as position P in Figs. 1, 2 and 5 , then $\mathrm{O}_{\mathrm{II}}-\mathrm{O}_{\mathrm{IV}}$ became $2.71 \AA$ and other distances involving $\mathrm{O}_{\mathrm{Iv}}$ moved closer to normal values (Table 6(a)); the mean deviation from the tetrahedral

Table 6(a). Changes in interatomic distances by altering position of $\mathrm{O}_{\mathrm{Iv}}$ from
$(0.650,0.145,0.970)$ to $(0.695,0.145,0.945)$
Distances obtained Distances obtained from Fourier maps with new parameters

|  | $2.56 \AA$ | 2.81 |
| :--- | ---: | :--- |
| $\mathrm{Ba}_{\mathrm{I}}-\mathrm{O}_{\mathrm{IV}}$ | 2.67 | 2.74 |
| $\mathrm{Ba}_{\mathrm{I}} \mathrm{O}_{\mathrm{IV}}$ | 3.64 | 3.33 |
| $\mathrm{Ba}_{\mathrm{I}} \mathrm{O}_{\mathrm{IV}}$ | 3.08 | 2.80 |
| $\mathrm{Ba}_{\mathrm{II}}-\mathrm{O}_{\mathrm{IV}}$ | 3.39 | 3.20 |
| $\mathrm{Ba}_{\mathrm{II}}-\mathrm{O}_{\mathrm{IV}}$ | 1.63 | 1.75 |
| $\mathrm{~T}-\mathrm{O}_{\mathrm{IV}}$ | 3.12 | 3.15 |
| $\mathrm{O}_{\mathrm{I}}-\mathrm{O}_{\mathrm{IV}}$ | 2.38 | 2.71 |
| $\mathrm{O}_{\mathrm{II}}-\mathrm{O}_{\mathrm{IV}}$ | 3.51 | 3.52 |
| $\mathrm{O}_{\mathrm{II}}-\mathrm{O}_{\mathrm{IV}}$ | $>4.00$ | 3.81 |
| $\mathrm{O}_{\mathrm{II}}-\mathrm{O}_{\mathrm{IV}}$ | 2.79 | 2.79 |
| $\mathrm{O}_{\mathrm{II}}-\mathrm{O}_{\mathrm{IV}}$ | 2.98 | 3.51 |
| $\mathrm{O}_{\mathrm{IV}}-\mathrm{O}_{\mathrm{IV}}$ |  |  |

Table 6(b). Changes in angles in $\mathrm{TiO}_{4}$ tetrahedron

|  | Angles obtained <br> from Fourier maps | Angles obtained <br> with new parameters |
| :---: | :---: | :---: |
| $\mathrm{O}_{\mathrm{I}}-\mathrm{Ti}_{\mathrm{i}-\mathrm{O}_{\mathrm{IV}}}$ | $129^{\circ}$ | $124^{\circ}$ |
| $\mathrm{O}_{\mathrm{II}}-\mathrm{Ti}-\mathrm{O}_{\mathrm{IV}}$ | 94 | 106 |
| $\mathrm{O}_{\mathrm{III}}-\mathrm{Ti}-\mathrm{O}_{\mathrm{IV}}$ | 111 | 106 |

angle changed from $8.5^{\circ}$ to $6.0^{\circ}$ (Table $6(b)$ ). There is no evidence for such an atomic shift on the (100) projection while on the (001) projection, (Fig. 2), the two alternative positions for $\mathrm{O}_{\text {Iv }}$ are equally acceptable. Similarly, the corresponding sets of structure factors $F_{c}$ and $F_{c}^{\prime}$ in Tables $3(a)$ and $3(b)$ have $R$ factors which are not significantly different. It is evident that the estimated standard deviations of interatomic distances involving $\mathrm{O}_{\text {IV }}$ do not allow for inaccuracies resulting from serious overlap in projection.

The $\mathrm{Ba}-\mathrm{O}$ distances may be arbitrarily divided into two classes: oxygen atoms at distances less than $2.95 \AA$ are classed as nearest neighbours in contact with barium, and oxygen atoms at distances between $2.95 \AA$ and $3.55 \AA$ are classed as second-nearest neighbours. In making this division, it was noted that the sum of the Goldschmidt radii of Ba and O atoms is $2.75 \AA$ and the average $\mathrm{Ba}-\mathrm{O}$ distance in $\mathrm{BaTiO}_{3}$ is $2.84 \AA$. In $\mathrm{Ba}_{2} \mathrm{TiO}_{4}, \mathrm{Ba}_{1}$ is coordinated by ten oxygen atoms, five of which are nearest neighbours. The second barium, $B a_{\text {II }}$, is coordinated by eight oxygen atoms and is in contact with six of them;
when the revised position of $\mathrm{O}_{\text {IV }}$ is considered, $\mathrm{Ba}_{\text {II }}$ is in contact with seven oxygen atoms. For comparison, barium both in paracelsian, $\mathrm{BaAl}_{2} \mathrm{Si}_{2} \mathrm{O}_{8}$ (Smith, 1953) and in sanbornite, $\mathrm{Ba}_{2} \mathrm{Si}_{2} \mathrm{O}_{5}$ (Douglass, 1958) has nine oxygen neighbours, seven of which are in contact with the central barium atom.

## 6. Discussion

An important feature of the structure is that the atoms are loosely packed; in fact there is room for eight more oxygen atoms in the unit cell. In contrast to this, phases at the oxygen-rich end of the $\mathrm{BaO}-\mathrm{TiO}_{2}$ systems have structures derived from the close packing of oxygen atoms and the slightly larger barium atoms (Harrison, 1956a, 1956b); only octahedral intersticies between oxygen atoms are then available for the titanium atoms. Ferroelectric $\mathrm{BaTiO}_{3}$, however, has a distorted perovskite structure and is not perfectly close packed. Megaw (1957) has suggested that, even in this structure, the Ti atom shows some evidence of covalent bonding; the $\mathrm{O}-\mathrm{Ti}-\mathrm{O}$ angles in the oxygen octahedron differ from $180^{\circ}$ and there is a short Ti-O distance of $1.87 \AA$ (Frazer, Danner \& Pepinsky, 1955).

It is evident that for $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ and $\mathrm{BaTiO}_{3}$ the ratio of the number of oxygen atoms to barium atoms is not sufficient to allow a close packed framework, the effect being much more important in $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ than in $\mathrm{BaTiO}_{3}$. In $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$, the $\mathrm{Ti}-\mathrm{O}$ bond becomes the predominant factor which produces a tetrahedral environment around titanium, and the result is a loosely packed structure of barium atoms and $\mathrm{TiO}_{4}$ groups.

The atomic arrangement in $\mathrm{Sr}_{2} \mathrm{TiO}_{4}$ provides an example of the type of structure $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ might have if the barium atoms were slightly smaller. The radii of the strontium and oxygen atoms are nearly equal, with the result that $\mathrm{Sr}_{2} \mathrm{TiO}_{4}$ has a $\mathrm{K}_{2} \mathrm{NiF}_{4}$ type structure (Ruddlesden \& Popper, 1957), an arrangement of atoms derived from a cubic close-packed array of strontium and oxygen atoms. The structure is closely related to $\mathrm{SrTiO}_{3}$ and the titanium atom is octahedrally coordinated. At very low temperatures, however, the close-packing factor ceases to be overwhelming and some distortion is allowed; evidence for this is provided by the presence of an induced ferroelectric effect in $\mathrm{SrTiO}_{3}$ at $4^{\circ} \mathrm{K}$. (Gränicher, 1956).

## 7. Thermal behaviour of $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$

Since the crystallographic features of $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ and $\beta-\mathrm{Ca}_{2} \mathrm{SiO}_{4}$ are similar, it is natural to expect that $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ may show polymorphic modifications similar to those observed in $\mathrm{Ca}_{2} \mathrm{SiO}_{4}$ (Bredig, 1950). Some support for this suggestion comes from the work of Todd \& Lorenson (1952). They showed that, as the temperature is increased, the heat capacity of $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ approaches a peak in the region of room temperature while the heat capacity of $\mathrm{Sr}_{2} \mathrm{TiO}_{4}$ shows no unusual type of variation with temperature. This could mean
that $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ undergoes at least one phase change above room temperature.

Midgley (1952) has suggested that the structures of the high-temperature modifications of $\mathrm{Ca}_{2} \mathrm{SiO}_{4}$ may be derived from the $\beta$-phase by rotating the $\mathrm{SiO}_{4}$ tetrahedra. This may not happen with $\mathrm{Ba}_{2} \mathrm{TiO}_{4}$ for it is not possible to predict the effect of a temperature change on the $\mathrm{Ti}-\mathrm{O}$ bond. If it ceases to be stronger than the other bonds then it is more likely that there will be a reconstructive change to a more close packed arrangement such as the $\mathrm{Sr}_{2} \mathrm{TiO}_{4}$ structure.

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# The Crystal Structure of Barbituric Acid Dihydrate 

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#### Abstract

Barbituric acid dihydrate, $\mathrm{C}_{4} \mathrm{H}_{4} \mathrm{~N}_{2} \mathrm{O}_{3} .2 \mathrm{H}_{2} \mathrm{O}$, forms crystals which have a hydrogen-bonded layer structure in which the barbituric acid and water molecules lie on the mirror planes of the space group Pnma. The barbituric acid is in the tri-keto form and, within the accuracy of the analysis, has $m m$ symmetry. The water molecules are hydrogen-bonded in pairs and their hydrogen-bond coordination is unusual in that it is planar and approximately trigonal. The structure analysis was refined by isotropic and anisotropic least squares methods.


## Introduction

Barbituric acid, $\mathrm{C}_{4} \mathrm{H}_{4} \mathrm{~N}_{2} \mathrm{O}_{3}$, is the parent compound for a wide variety of derivatives famous for their drug action. A recent compilation (Blicke \& Cox, 1959) listed several hundred such compounds, under the general classification as 'barbiturates', which had been synthesized and examined with respect to their pharmacological activity.

[^1]The structural interest in the molecule of barbituric acid itself, I, lies in its behaviour as a carboxylic acid comparable in strength with formic and benzoic acids. This acidity ( $K_{a}=1.0 \times 10^{-4}$ ) is apparently associated with the particular combination of the active methylene group of the malonyl system with the potential imino carboxylic configuration of urea, since comparable acidity is not shown either by the malonyl esters or urea derivatives separately or by related cyclic compounds such as isobarbituric acid, II, ( $K_{a}=2.5 \times 10^{-9}$ ), alloxan, III, ( $K_{a}=2.3 \times 10^{-7}$ ), and diketopiperazine, IV.


[^0]:    * Estimates of reasonable limits of experimental error are

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